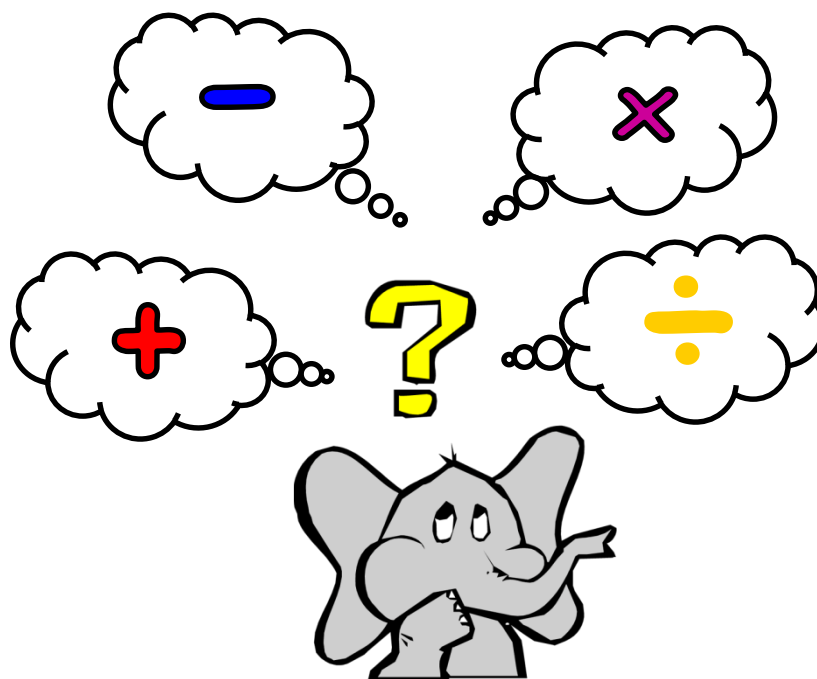


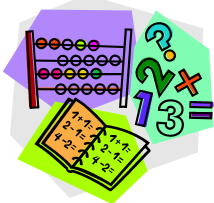
Progression in Calculations

Informal Curriculum 4 - 8

Formal Curriculum 8 - 15



Two Rivers Primary School

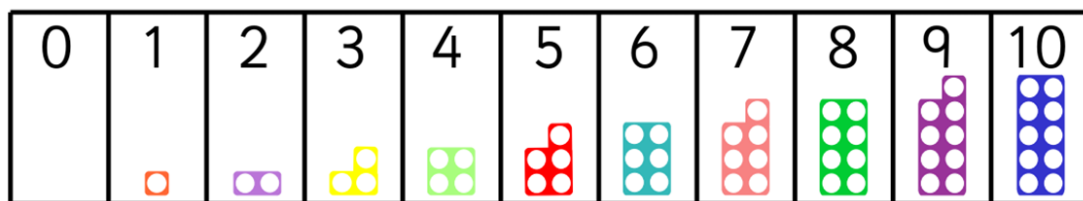


Introduction

The maths work your child is doing at school initially starts with practical applications to develop a good basis of mental maths skills - these skills are learnt through, actions, songs, repetition and the use of equipment. At Two Rivers School we ensure that these skills are learnt and developed on a daily basis in real life and practical situations.

This booklet is designed to inform you about the progression in calculation methods that we use at Two Rivers Primary for addition, subtraction, multiplication and division.

Later when children are taught more formal written methods they are encouraged to use these methods for calculations they cannot solve in their heads. We use Numicon to support our access and learning across the whole school.

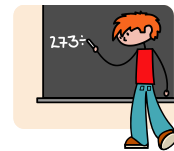


Written methods of calculations are based on mental strategies. Each of the four operations builds on mental skills which provide the foundation for jottings and informal written methods of recording. Skills need to be taught, practised and reviewed constantly. These skills lead on to more formal written methods of calculation when the children are ready for them. For many children this will be in the later years of primary school or into secondary school.

Strategies for calculation need to be supported by familiar models and images to reinforce understanding. When teaching a new strategy it is important to start with numbers that the child can easily manipulate so that they can understand the concept.

The transition between stages should not be hurried as not all children will be ready to move on to the next stage at the same time, therefore the progression in this document is outlined in stages. Previous stages may need to be revisited to consolidate understanding when introducing a new strategy.

A sound understanding of the number system is essential for children to carry out calculations efficiently and accurately.



By the end of year 6, children will have a range of calculation methods, mental and written. Selection will depend upon the numbers involved. Discussing the efficiency and suitability of different strategies is important.

Remember that the expanded methods are perfectly good ways of working out an answer if the children feel more comfortable and therefore find it easier. They give the same answer and it can often be quicker if they are confident about what they are doing.

These methods are very useful when children are extending their work, for example to numbers involving decimals.

Children should not be made to go onto the next stage if:

- they are not ready.
- they are not confident.



Mental calculation

Developing confidence and efficiency in mental calculations is a vital part of Maths teaching throughout Key Stage 2.

Regular practice of number facts is important both at school and at home. Any opportunities to practise are very useful, for example through **real life situations** such as shopping as well as activities such as games.

The children would greatly benefit from knowing key number facts by heart and recalling them instantly (*e.g. number bonds to 10, tables*).

There are many useful games on the internet which give children chance to practise number facts and mental calculations.

For example, Hit the Button is good for practising number bonds and tables facts.

Children can access Education City at home which has a selection of basic number facts games to explore.

Multiplication Facts

Remember that truly **knowing** tables is not the same as just being able to count up in steps of a given number or being able to recite the table.

Really knowing a table means that the children can instantly tell you any fact up to $10\times$. It also means knowing the corresponding division facts.

For example, a child who knows the $3\times$ table well would be able to answer questions like these with very little hesitation:

9×3 , 7 lots of 3, 3×4 , $18\div 3$, how many 3s in 24?

As the children get more confident they should also have strategies for using known facts to help them work out other facts and also to work with larger numbers or decimals.

e.g. I know 5×3 is 15, so I can work out 50×3 , 5×30 , $150\div 5$, 500×3 , 50×30 , 5×0.3 , $150\div 30$...

A suggested order for learning tables:

$2\times$, $10\times$, $5\times$, $4\times$ (double $2\times$), $3\times$, $6\times$ (double $3\times$), $9\times$, $8\times$, $7\times$

At Two Rivers this becomes part of our 20:20 sessions.

**Just a few minutes a day
could make a real
difference to your child's
confidence with number.**



ICT links

There are many useful games on the internet which give children chance to practise number facts and mental calculations.

For example, **Hit the Button** is good for practising number bonds and tables facts.

You can also access a selection of basic number facts games on **Education City**.

Other useful sites include:

www.topmarks.co.uk select Games, 7-11 then category e.g. addition and subtraction

www.bbc.co.uk/schools/ks2bitesize/maths (particularly useful for Y6)

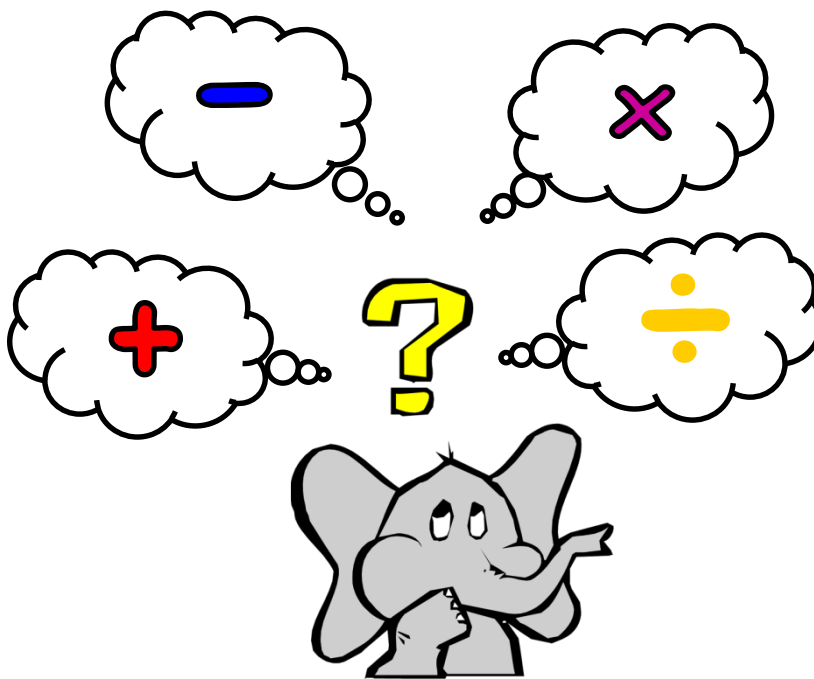
www.ictgames.com (select numeracy - designed for infants but some useful games to practise basic number facts)

mathsframe.co.uk/en/resources/category/22/most-popular

[Numberblocks - CBeebies – BBC](http://Numberblocks-CBeebies-BBC)

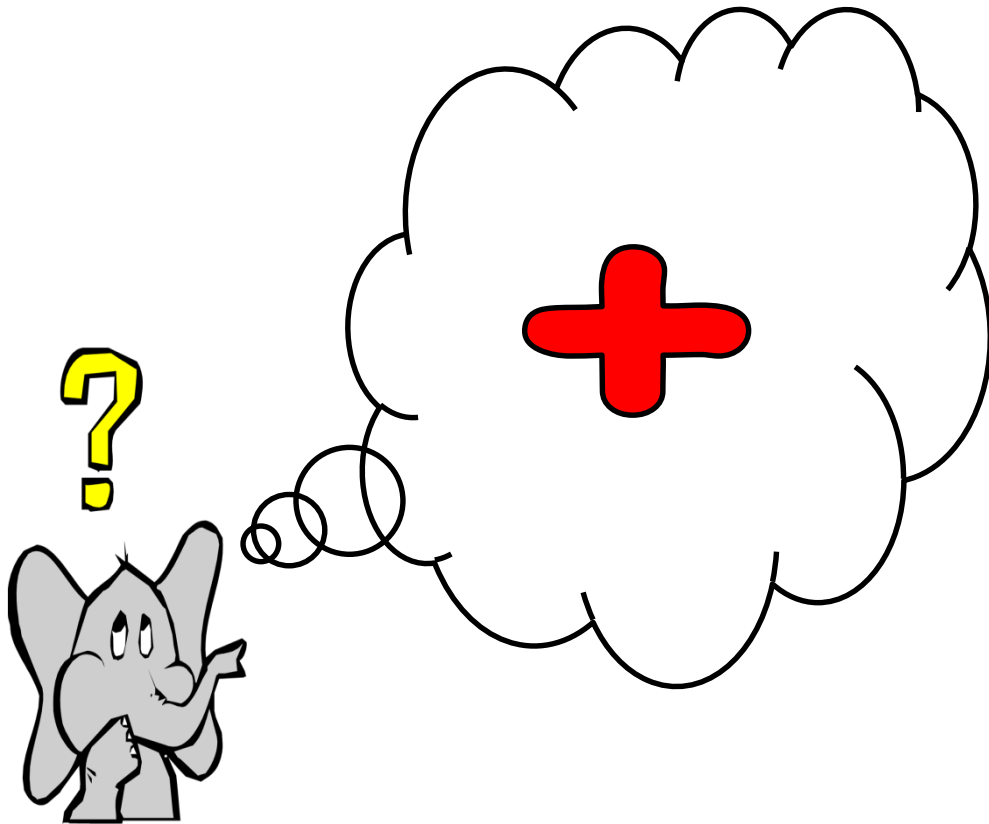
Progression in Calculations

Informal Curriculum 4 - 8



Two Rivers Primary School

Addition



add and count on
addition plus
more sum total
altogether increase

Recognise numbers 0 to 10

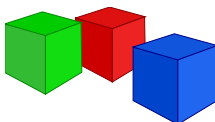
0 1 2 3 4 5 6 7 8 9 10



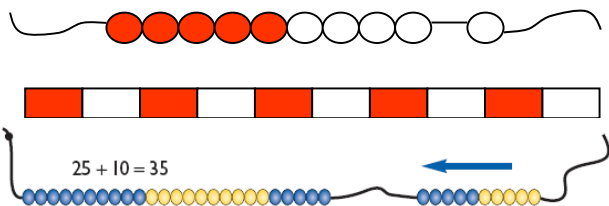
1, 2, 3, 4, 5, 6
... there are 6
teddies

Count reliably up to 10 everyday objects

Find one more than a number



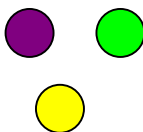
One more than
three is four



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Count in ones and tens

Begin to relate addition to
combining two groups of objects



and makes 5

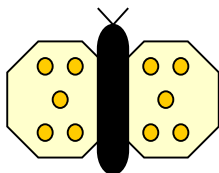
$$3 + 2 = 5$$



Count along a number line to
add numbers together

Begin to use the + and = signs to record
mental calculations in a number sentence

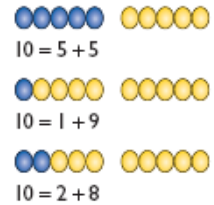
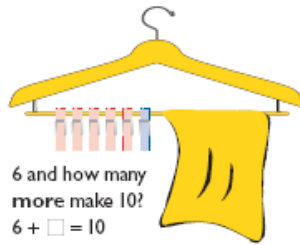
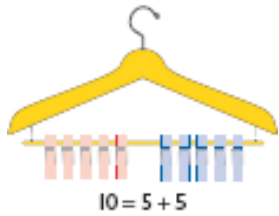
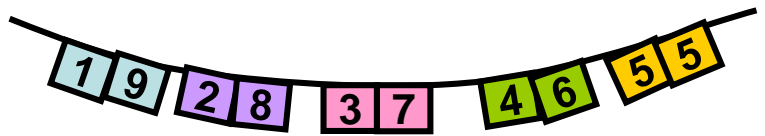
$$6 + 4 = 10$$



$$5 + 5 = 10$$

Know doubles of numbers

Know by heart all pairs of numbers with a total of 10



$$1 + 2 = 3$$



$$2 + 1 = 3$$



$$2 + 5 = 7$$

2 count on 5



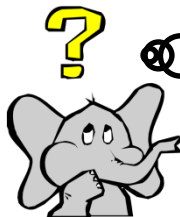
$$5 + 2 = 7$$

5 count on 2

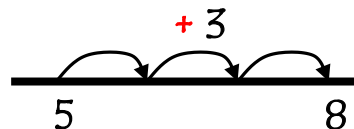


Know that addition can be done in any order

Put the biggest number first and count on

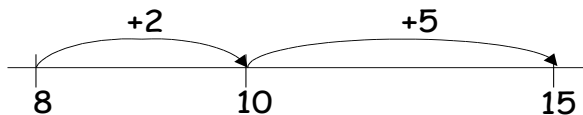


$$3 + 5$$



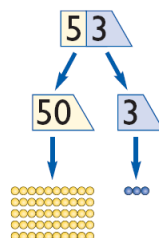
Next Steps...

$$8 + 7 = 15$$



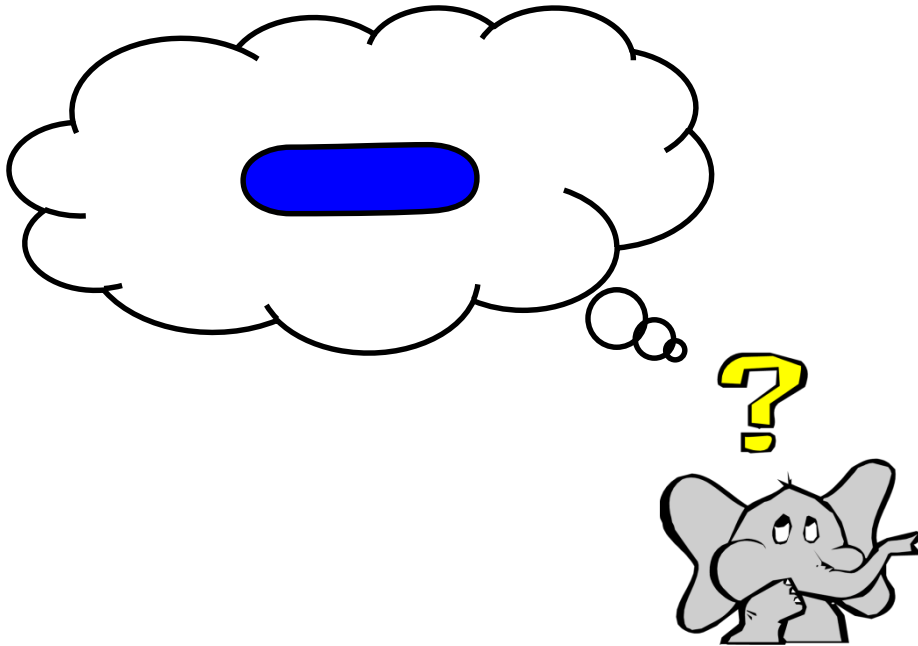
Add two single-digit numbers that bridge 10

Begin to partition numbers in order to add



$$30p + 4p = 34p$$

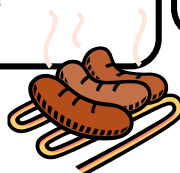
Subtraction



count back take away
fewer subtract
minus less
difference between

Begin to count backwards in familiar contexts such as number rhymes or stories

Five fat sausages frying in a pan ...



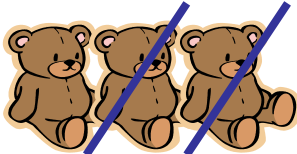
Ten green bottles hanging on the wall ...



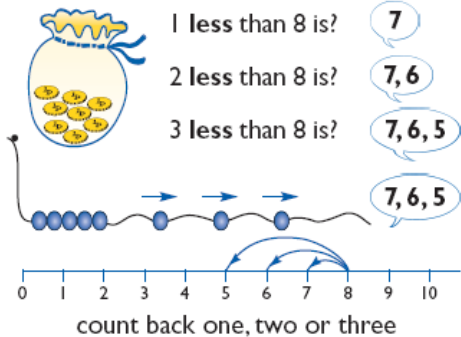
10, 9, 8, 7, ...

Continue the count back in ones from any given number

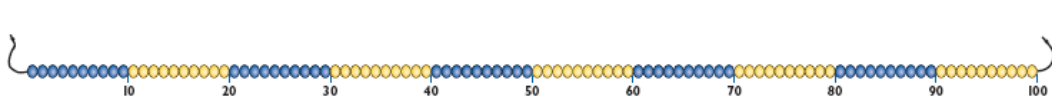
Begin to relate subtraction to 'taking away'



Three teddies **take away** two teddies leaves one teddy



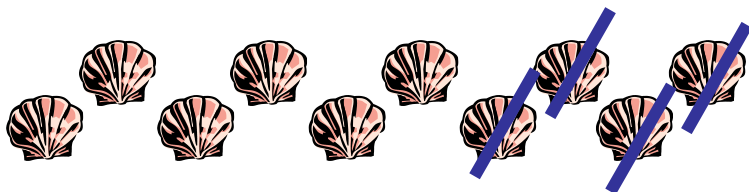
Find one less than a number



Count back in tens



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100



If I **take away** four shells there are six left



Count backwards along a number line to 'take away'

Begin to use the - and = signs to record mental calculations in a number sentence

Maria had six sweets and she ate four. How many did she have left?



?



$$6 - 4 = 2$$



$$6 + ? = 10$$

$$10 - 6 = ?$$

$$? + 6 = 10$$

$$10 - 4 = 6$$



$$20 = 12 + 8$$

$$8 + 12 = 20$$

$$20 - 8 = 12$$

$$20 - 12 = 8$$

Know by heart subtraction facts for numbers up to 10 and 20

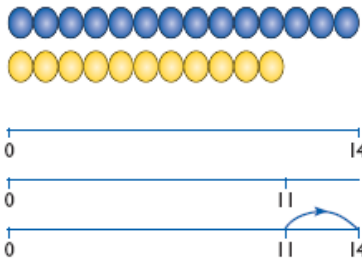
Next Steps...

Subtract single digit numbers often bridging through 10

$$15 - 7 = 8$$



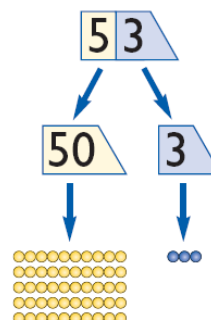
The difference is?



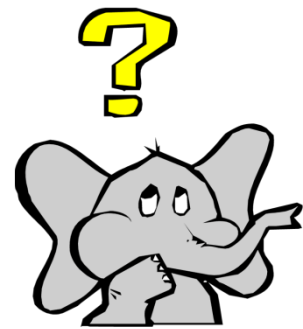
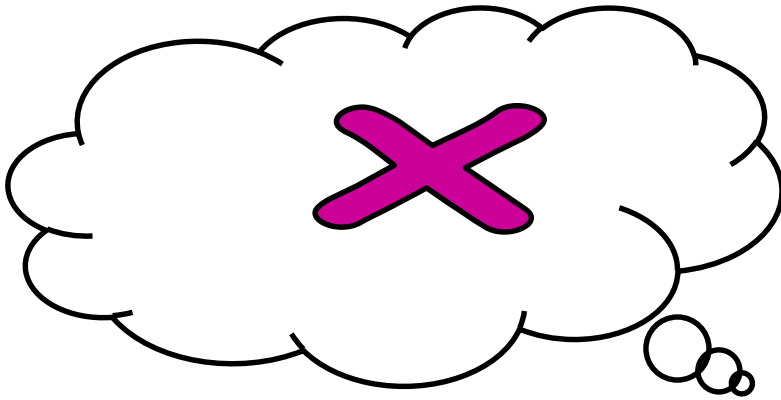
The difference between 11 and 14 is 3.
 $14 - 11 = 3$
 $11 + \square = 14$

Begin to find the difference by counting up from the smallest number

Begin to partition numbers in order to take away



Multiplication



multiplication

product

once, twice, three times

double groups of

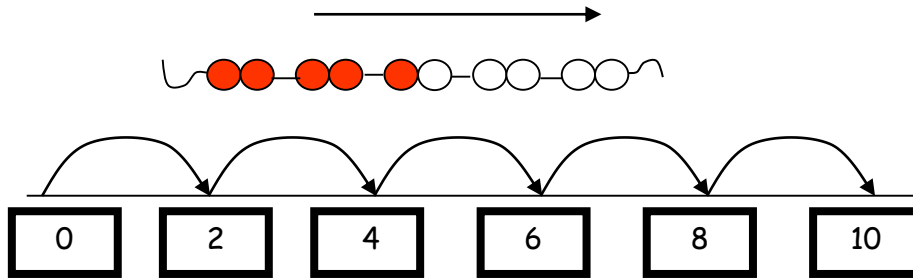
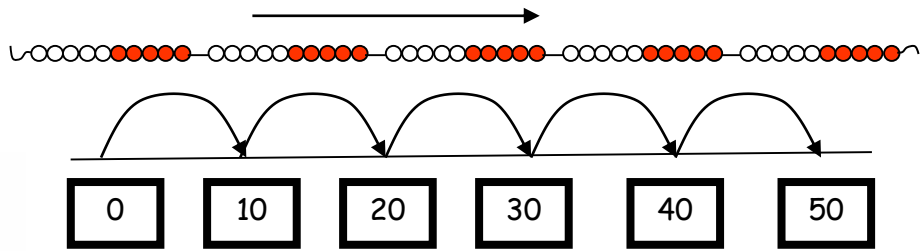
repeated addition lots of

array, row, column multiply

times

multiple

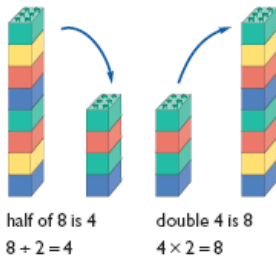
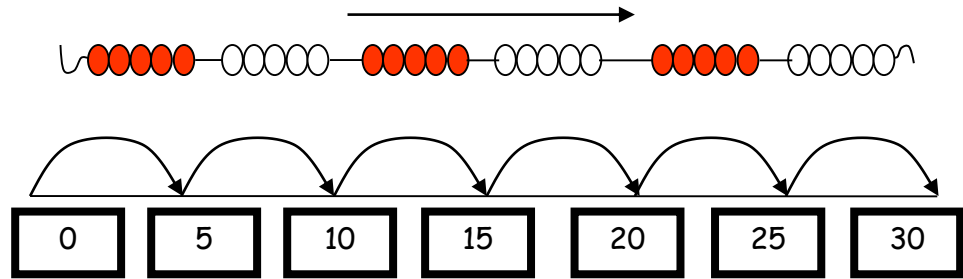
Count in tens
from zero



Count in twos
from zero



Count in fives
from zero



Know doubles and
corresponding halves

Know multiplication tables to 10×10

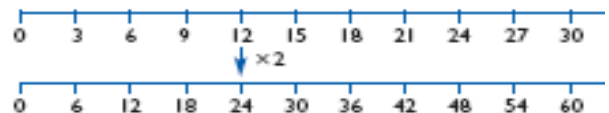
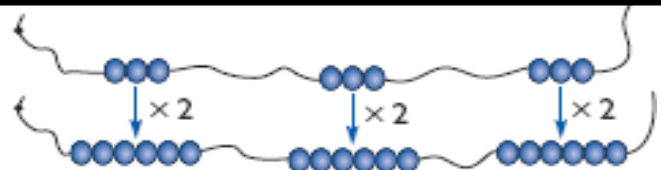
$$2 \times 5 = 10$$

$$\times 5$$

$$6 \times 5 = 30$$

$$3 \times 5 = 15$$

$$8 \times 5 = 40$$

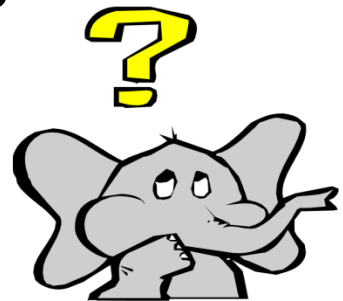
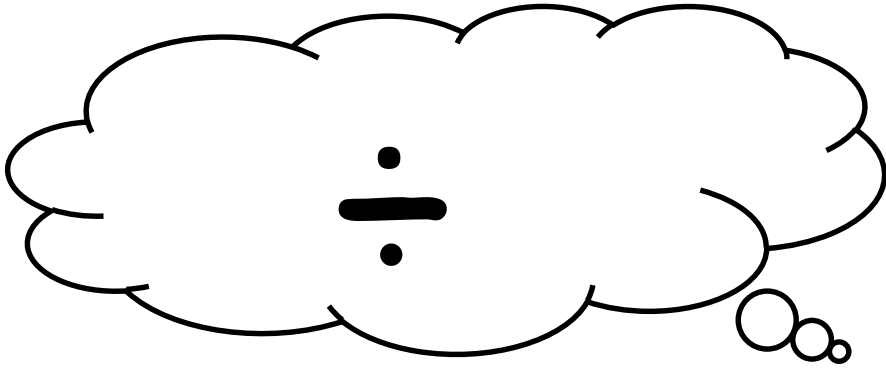


$$12 \times 2 = 24$$

Twice as
many

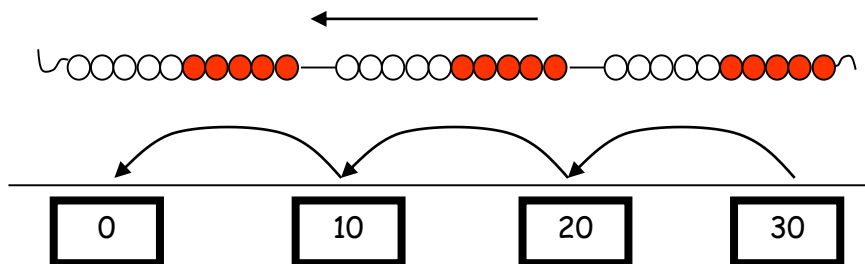
Use known facts to
work out new ones

Division

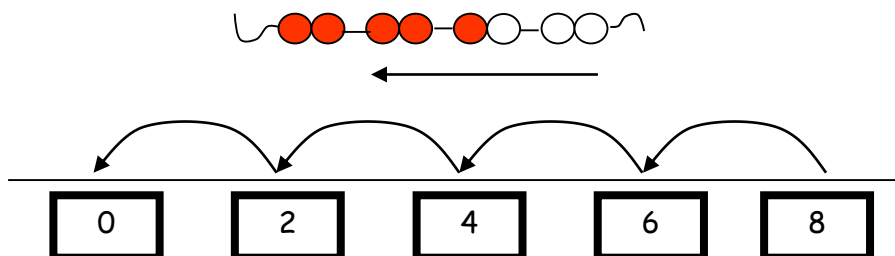


group groups of
 lots of divide
divided by quotient
division factor
 remainder divisible
half halve share

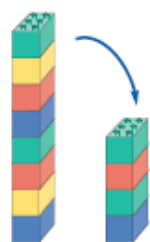
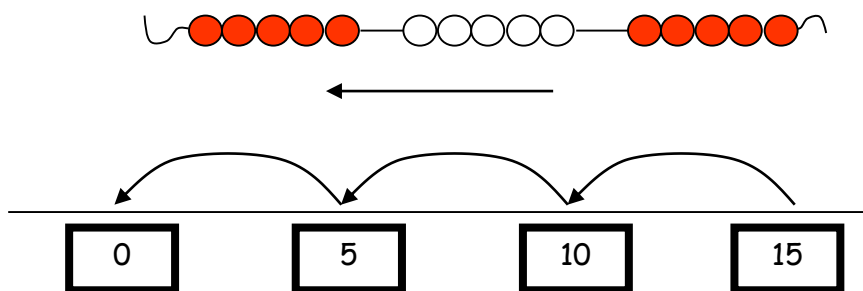
Count back in tens



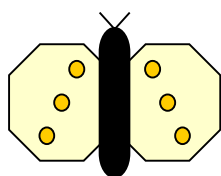
Count back in twos



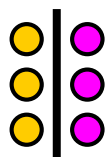
Count back in fives



half of 8 is 4
 $8 \div 2 = 4$



Half of 6 is 3
 $\frac{1}{2}$ of 6 = 3



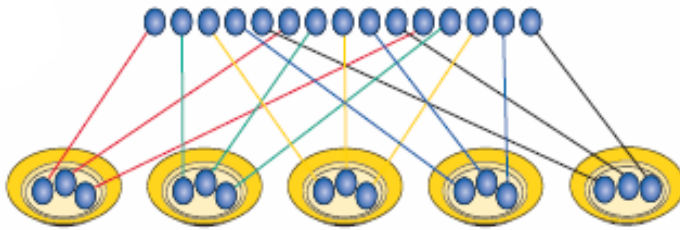
Know halves

Use known multiplication facts to work out corresponding division facts

If $2 \times 10 = 20$
then
 $20 \div 10 = 2$
 $20 \div 2 = 10$

$$15 \div 5 = 3$$

15 shared between 5



Understand division
as sharing

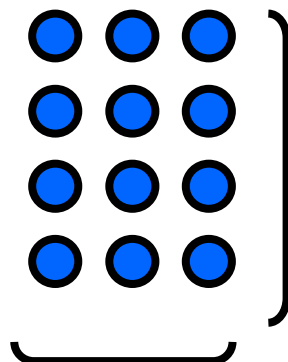
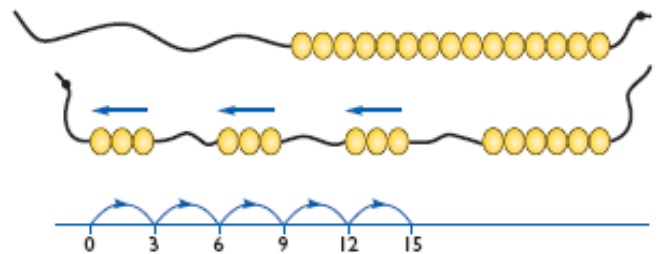
Next Steps...

Understand division
as grouping

How many 3s
in 15?



$$15 \div 3 = 5$$



12 divided into groups
of 3 gives 4 groups

$$12 \div 3 = 4$$

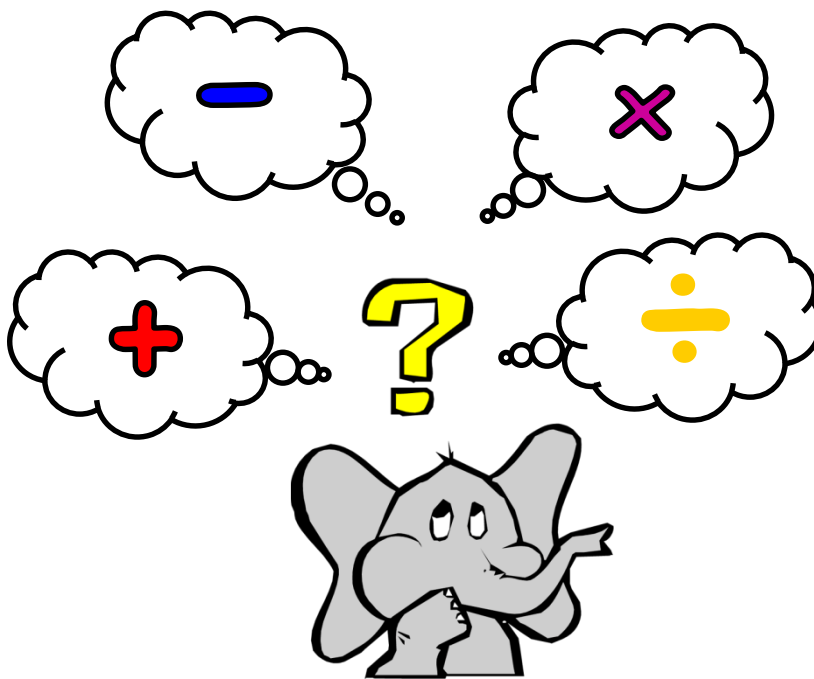
12 divided into groups
of 4 gives 3 groups

$$12 \div 4 = 3$$

Reinforce division as
grouping through the
use of arrays

Progression in Calculations

Formal Curriculum 8 - 15



Two Rivers Primary School

Addition and subtraction are inverse operations. Right from the start children should be taught these as related operations. There are four number sentences (two using + and two using -) which can be written to express the relationship between 4 and 6 and 10. It is key to a good understanding of addition and subtraction that $6 + [] = 10$ and $10 - 6 = []$ are seen as ways of expressing the same question.

+ Addition

Using place value

Count on in ones/ counting in tens, eg. knowing $45 + 1$ or $45 + 10$ without counting on in ones.



$$45 + \square = 50 \quad 65 + \square = 70$$

$$85 + \square = 90$$

Bead strings and 1-100 number grid help counting on/back in tens.

- Subtraction

Using place value

Count back in 1s/Count back in 10s. Say one less than any number to 100. Say 10 less without counting back in ones.

$$33 - 10 = 23$$

1	2	3	4	5
11	12	13	14	15
21	22	23	24	25
31	32	33	34	35
41	42	43	44	45

Subtracting by taking away

Count back in ones, eg. $15 - 3 = 12$ or $25 - 3 = 22$



Count back in tens.



Using number facts

Story of 4, 5, 6, 7, 8 and 9, eg. $7 = 7 + 0$ or $6 + 1$ or $5 + 2$ or $4 + 3$. Number bonds to 10, eg. $5 + 5$, $6 + 4$, $7 + 3$, $8 + 2$, $9 + 1$, $10 + 0$.



$$6 + \square = 10$$



$$5 + \square = 10$$



$$7 + \square = 10$$

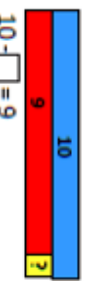


$$9 + \square = 10$$

Missing number sentences, $3 + [] = 7$, link addition and subtraction.



$$10 - \square = 7$$



$$10 - \square = 9$$

Patterns using known facts, eg. $4 + 3 = 7$ so we know $24 + 3$, $44 + 3$, $74 + 3$, etc.

Patterns using known facts, eg. $10 - 7 = 3$ so we know $30 - 7 = ?$



Addition and subtraction are inverse operations. Right from the start children should be taught these as related operations. There are four number sentences (two using + and two using -) which can be written to express the relationship between 4 and 6 and 10. It is key to a good understanding of addition and subtraction that $6 + [] = 10$ and $10 - 6 = []$ are seen as ways of expressing the same question.

+ Addition

Using place value

Know 1 more or 10 more than any number, e.g. 1 more than 67 or 10 more than 85.

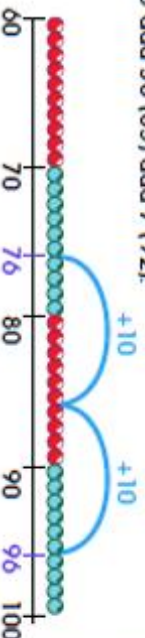
Partitioning, e.g. $55 + 37$
as $50 + 30$ and $5 + 7$
finally combining the two totals: $80 + 12$

$$\begin{array}{r} 50 \\ + 30 \\ \hline 80 \end{array} \quad \begin{array}{r} 5 \\ + 7 \\ \hline 12 \end{array} \quad \begin{array}{r} 80 \\ + 12 \\ \hline 92 \end{array}$$

Bead strings and 1-100 number grid help counting on/back in tens.

Counting on

Add ten and multiples of ten, e.g. $76 + 20$ as $76, 86, 96$ or in one hop $76 + 20$. Add two 2-digit numbers by counting on in tens and then in ones, e.g. $55 + 37$ as 55 add 30 (85) add 7 (92).

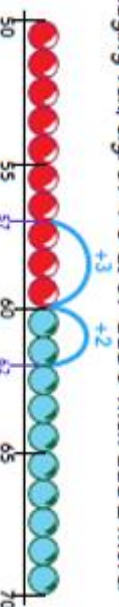


Add near multiples, e.g. $46 + 19$ or $63 + 21$.

Using number facts

Know pairs of numbers which make the numbers up to and including 10, e.g. $8 + 4, 3 + 5, 2 + 8, 1 + 9$ and $10 = 5 + 5, 4 + 6, 3 + 7, 2 + 8, 1 + 9, 0 + 10$. Patterns of known facts, e.g. $6 + 3 = 9$, so we know $36 + 3 = 39$, $66 + 3 = 69$, $53 + 6 = 59$.

Bridging ten, e.g. $57 + 5$ as 57 add 3 then add 2 more.



Missing number sentences, $3 + [] = 7$, link addition and subtraction.

Adding three or more single-digit numbers, spotting bonds to 10 or doubles, e.g. $6 + 7 + 4 + 2$ as $10 + 7 + 2$

- Subtraction

Using place value

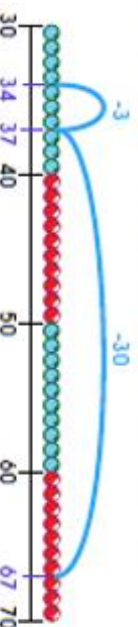
Know 1 less or 10 less than any number, e.g. 1 less than 74 or 10 less than 82.

Partitioning, e.g. $55 - 32$ as $50 - 30$ and $5 - 2$ combining the answers: $20 + 3$.

$$\begin{array}{r} 50 \\ - 30 \\ \hline 20 \end{array} \quad \begin{array}{r} 5 \\ - 2 \\ \hline 3 \end{array} \quad \begin{array}{r} 20 \\ + 3 \\ \hline 23 \end{array}$$

Taking away

Subtract ten and multiples of ten, e.g. $76 - 20$ as $76, 66, 56$ or in one hop $76 - 20 = 56$. Subtract two 2-digit numbers by counting back in tens then in ones, e.g. $67 - 33$ as 67 subtract 30 (37) then count back 3 (34).

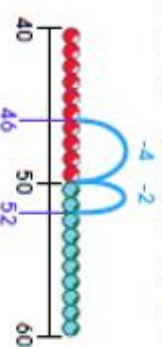


Subtracting near multiples, e.g. $74 - 21$ or $57 - 19$.

Using number facts

Know pairs of numbers which make the numbers up to and including 10, e.g. $10 - 6 = 4$, $8 - 3 = 5$, $5 - 2 = 3$, etc. Patterns of known facts, e.g. $9 - 6 = 3$, so we know $39 - 6 = 33$, $69 - 6 = 63$, $89 - 6 = 83$.

Bridge ten, e.g. $52 - 6$ as 52 subtract 2 then subtract 4 more.



Counting up

Find a difference between two numbers on a line, e.g. $51 - 47$.

Addition and subtraction are inverse operations. Right from the start children should be taught these as related operations. There are four number sentences (two using + and two using -) which can be written to express the relationship between 4 and 6 and 10. It is key to a good understanding of addition and subtraction that $6 + [] = 10$ and $10 - 6 = []$ are seen as ways of expressing the same question.

+ Addition

Using place value

Count in hundreds, e.g. knowing $475 + 200$ as $475, 575, 675$.

Add multiples of 10, 100 and £1.

e.g. $746 + 200$ or $746 + 40$ or $£6.34 + £5$ as $£6 + £5$ and $34p$.

Partitioning, e.g. $68 + 74$ as $60 + 70$ and $8 + 4$ and

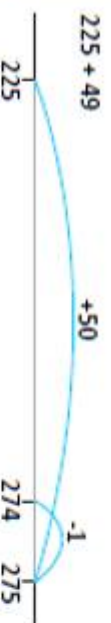
combine the totals: $130 + 12 = 142$

Or $£8.50 + £3.70$ as $£8 + £3$ and $50p + 70p$ and combine: $£11 + £1.20$.

Counting on

Add 2-digit numbers by adding the multiple of ten then the ones, e.g. $67 + 55$ as 67 add 50 (117) add 5 (122).

Add near multiples of 10 and 100, e.g. $67 + 39$ or $364 + 199$.



Count on from 3-digit nos, e.g. $247 + 34$ as $247 + 30$ (277) then $277 + 4 = 281$.

Using number facts

Number bonds to 100, e.g. $35 + 65, 46 + 54, 73 + 27$, etc.

	100
65	35

Add to next ten and next hundred, e.g. $176 + 4 = 180, 435 + 65 = 500$, etc.

- Subtraction

Taking away

Use place value to subtract, e.g. $358 - 300$ or $348 - 40$ or $348 - 8$. Taking away multiples of 10, 100 and £1, e.g. $476 - 40 = 436$.

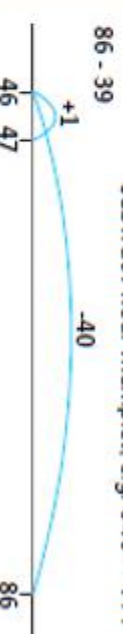
$476 - 300 = 176, £4.76 - £2 = £2.76$.

Partitioning, e.g. $68 - 42$ as $60 - 40$ and $8 - 2$ or $£6.84 - £2.40$ as $£6 - £2$ and $80p - 40p$.

Count back in hundreds, tens and then ones.

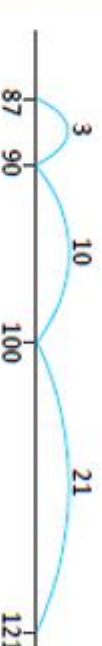
e.g. $763 - 121$ as $763 - 100$ (663) then subtract 20 (643) then subtract 1 (642).

Subtract near multiples, e.g. $648 - 199$ or $86 - 39$.



Counting up

Find a difference between two numbers by counting up from the smaller to the larger, e.g. $121 - 87$.



Using number facts

Number bonds to 100, e.g. $100 - 35 = 65, 100 - 48 = 52$, etc.

	100
48	?

We no longer count in 1s but use PV and number facts.

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+ Written Addition

Written method:

Build on partitioning to develop expanded column addition with two 3-digit numbers.

$$\begin{array}{r} 400 \quad 60 \quad 6 \\ + 300 \quad 50 \quad 8 \\ \hline 700 \quad 110 \quad 14 \end{array}$$

Expanded column addition with 'carrying'.

$$\begin{array}{r} 400 \quad 60 \quad 6 \\ + 300 \quad 50 \quad 8 \\ \hline 100 \quad 10 \quad 14 \\ \hline 800 \quad 20 \quad 4 \end{array}$$

Compact column addition with two or more 3-digit numbers or towers of 2-digit numbers.

$$\begin{array}{r} 347 \\ 286 \\ + 495 \\ \hline 21 \\ \hline 1128 \end{array}$$

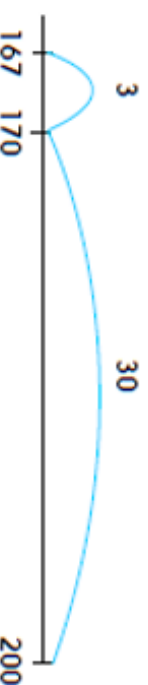
Compact column addition with 3-digit numbers

Recognise fractions which add to 1, e.g. $\frac{1}{4} + \frac{3}{4}$ or $\frac{2}{5} + \frac{3}{5}$.

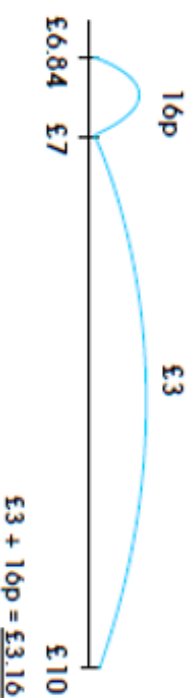
- Written Subtraction

Develop counting up subtraction.

Counting up subtraction is a crucial mental strategy.



Use counting up subtraction to find change from £1 and £10.



Recognise complements of any fraction to 1, e.g. $1 - \frac{1}{4} = \frac{3}{4}$ or $1 - \frac{2}{5} = \frac{3}{5}$.

Important to see the visual image of fractions totalling one whole.

Addition and subtraction are inverse operations. Right from the start children should be taught these as related operations. There are four number sentences (two using + and two using -) which can be written to express the relationship between 4 and 6 and 10. It is key to a good understanding of addition and subtraction that $6 + [] = 10$ and $10 - 6 = []$ are seen as ways of expressing the same question.

+ Addition

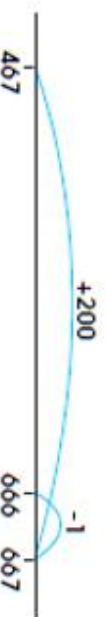
Using place value

Count in thousands, e.g. knowing $475 + 200$ as $475, 575, 675$.
Partitioning, e.g. $746 + 203$ as $700 + 200$ and $46 + 3$
or $134 + 707$ as $130 + 700$ and $4 + 7$.

PV and number facts are central to mental strategies.

Counting on

Add 2-digit numbers by adding the multiple of ten then the ones, e.g. $67 + 55$ as 67 add 50 (117) add 5 (122).
Add near multiples of 10, 100 and 1000, e.g. $467 + 199$ or $3462 + 2999$.



Count on to add 3-digit numbers and money, e.g. $463 + 124$ as $463 + 100$ (563) $+ 20$ (583) $+ 4 = 587$ or $£4.67 + £5.30$ as $£9.67$ add $30p$.

Using number facts

Number bonds to 100 and to next multiple of 100, e.g. $463 + 37, 1353 + 47$.

Number bonds to £1 and to the next whole pound, e.g. $£3.45 + 55p$.

Add to the next whole number, e.g. $4.6 + 0.4$ or $7.2 + 0.8$.

Counting up is essential for money calculations and, later, decimals.

- Subtraction

Taking away

Use place value to subtract, e.g. $4748 - 4000$ or $4748 - 8$, etc.

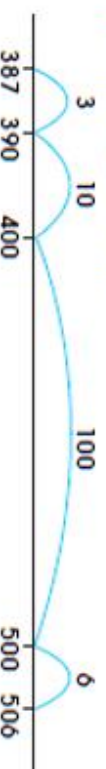
Take away multiples of 10, 100, 1000, £1, 10p or 0.1, e.g. $8392 - 50$ or $6723 - 3000$ or $£3.74 - 30p$ or $5.6 - 0.2$.

Partitioning, e.g. $£5.87 - £3.04$ as $£5 - £3$ and $7p - 4p$ or $7493 - 2020$ as $7000 - 2000$ and $90 - 20$.

Count back, e.g. $6482 - 1301$ as $6482 - 1000$, then -300 , then -1 (5181).
Subtract near multiples, e.g. $3522 - 1999$ or $£34.86 - £19.99$.

Counting up

Find a difference between two numbers by counting up from the smaller to the larger, e.g. $506 - 387$.



$100 + 10 + 6 + 3 = 119$

Using number facts

Number bonds to 10, 100 and derived facts, e.g. $100 - 76 = 24, 1.0 - 0.6 = 0.4$.

100	
76	24

Number bonds to £1 and £10,

e.g. $£1.00 - 86p = 14p$ or $£10 - £3.40 = £6.60$.

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+ Written Addition

Build on expanded column addition to develop compact column addition with larger numbers.

$$\begin{array}{r} 1000 \quad 400 \quad 60 \quad 8 \\ + 4000 \quad 800 \quad 60 \quad 6 \\ \hline 1000 \quad 100 \quad 10 \\ \hline 6000 \quad 300 \quad 30 \quad 4 \end{array}$$

Expanded methods firm up a robust understanding of place value.

Compact column addition with larger numbers.

$$\begin{array}{r} 5347 \\ 2286 \\ + 1495 \\ \hline 9128 \end{array}$$

Use expanded and compact column addition to add amounts of money.
eg. £3.24 + £2.58.

$$\begin{array}{r} \text{£}3 \quad 20\text{p} \quad 4\text{p} \\ \text{£}2 \quad 50\text{p} \quad 8\text{p} \\ \hline \text{£}5 \quad 70\text{p} \quad 12\text{p} \quad \text{£}5.82 \end{array} \quad \begin{array}{r} \text{£}3.24 \\ + \text{£}2.58 \\ \hline \text{£}5.82 \end{array}$$

Add like fractions, eg. $\frac{3}{8} + \frac{1}{8} + \frac{1}{8}$.

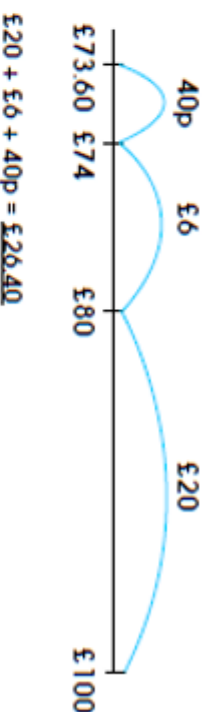
- Written Subtraction

Expanded column subtraction.

Begin to use column subtraction.

$$\begin{array}{r} 600 \quad 110 \quad 16 \\ - 260 \quad 20 \quad 8 \\ \hline 300 \quad 50 \quad 8 \end{array} \quad \begin{array}{r} 6 \quad 11 \quad 16 \\ - 3 \quad 2 \quad 8 \\ \hline 3 \quad 6 \quad 8 \end{array}$$

Use counting up subtraction to find change from £10, £20, £50 and £100.
eg. £100 - £73.60.



Subtract like fractions, eg. $\frac{3}{8} - \frac{1}{8} = \frac{2}{8}$.

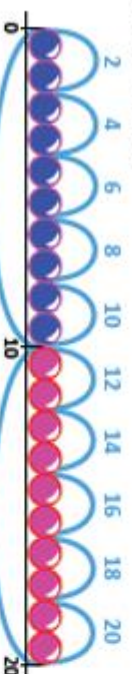
Stress that decimals and fractions are parts of a whole.

Multiplication and division are inverse operations. Right from the start children should be taught these as related operations. There are four number sentences (two using \times and two using \div which can be written to express the relationship between 5 and 9 and 45. It is key to a good understanding of division that $\square \times 5 = 45$ and $45 \div 5 = \square$ are seen as ways of expressing the same question.

\times Multiplication

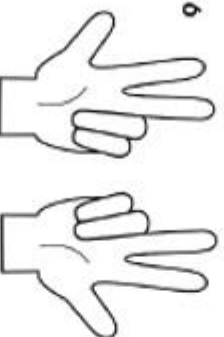
Counting in steps ['Clever' counting]

Count in 2s and 10s.



Doubling and halving

Find doubles to double 6 using fingers.



'Clever' counting is an excellent basis for multiplication and division.

Grouping
Begin to use visual and concrete arrays and 'sets of' objects to find the answers to '3 lots of 4' or '2 lots of 5', etc.

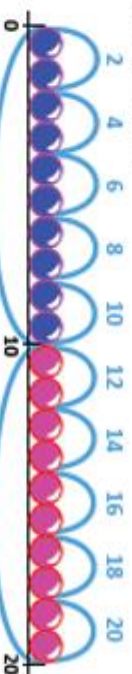


Division must be presented as the inverse of multiplication (grouping).

\div Division

Counting in steps ['Clever' counting]

Count in 2s, and 10s.



Doubling and halving

Find half of even numbers up to 12 including realising that it is hard to halve an odd number.

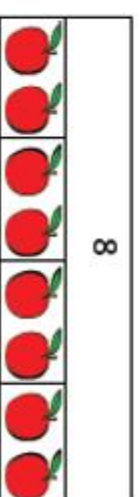


Grouping

Begin to use visual and concrete arrays and 'sets of' objects to find the answers to 'how many towers of 3 can I make with 12 cubes?'

Sharing

Begin to find half of a quantity using sharing, e.g. half of 16 cubes by giving one each repeatedly to two children.

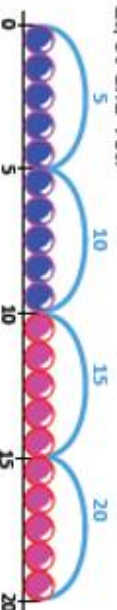


Multiplication and division are inverse operations. Right from the start children should be taught these as related operations. There are four number sentences (two using \times and two using \div which can be written to express the relationship between 5 and 9 and 45. It is key to a good understanding of division that $\square \times 5 = 45$ and $45 \div 5 = \square$ are seen as ways of expressing the same question.

\times Multiplication

Counting in steps ('Clever' counting)

Count in 2s, 5s and 10s.



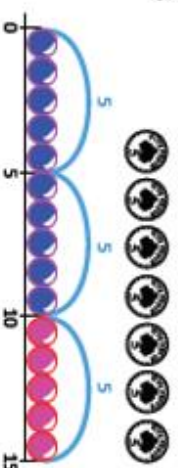
Begin to count in 3s.

'Clever' counting is an excellent basis for multiplication and division.

\div Division

Counting in steps ('Clever' counting)

Count in 2s, 5s and 10s

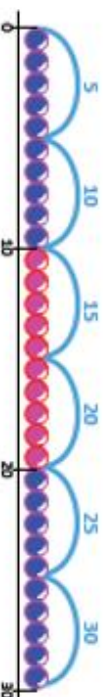
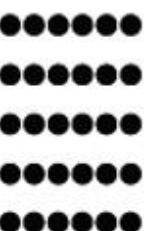


Doubling and halving

Begin to know doubles of multiples of 5 to 100.
e.g. double 35 is 70.

Grouping

Use arrays to find answers to multiplication and relate to 'clever' counting.
e.g. 3×4 as three lots of four things and 6×5 as six steps in the 5s count as well as six lots of five.



Understand that 5×3 can be worked out as three 5s or five 3s.

Use number facts

Know doubles to double 20

$$\text{Double } 7 = 14$$



Division, grouping, is the inverse of multiplication.

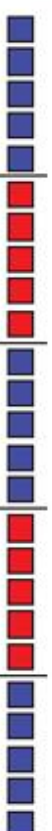
Start learning $2\times$, $5\times$, $10\times$ tables, relating these to 'Clever counting' in 2s, 5s, and 10s, e.g. $5 \times 10 = 50$, and 10, 20, 30, 40, 50 is five steps in the tens count.

Doubling and halving

Find half of numbers up to 40, including realising that half of an odd number gives a remainder of 1 or an answer containing a $\frac{1}{2}$.
Begin to know half of multiples of 10 to 100, e.g. half of 70 is 35.

Grouping

Relate division to multiplication by using arrays of towers of cubes to find answers to division, e.g. how many towers of five cubes can I make from 20 cubes as $\square \times 5 = 20$ and also as $20 \div 5 = ?$



Relate division to 'clever' counting and hence to multiplication, e.g. how many 5s do I count to get to 20?

Sharing

Begin to find half or a quarter of a quantity using sharing, e.g. $\frac{1}{4}$ of 16 cubes by sorting the cubes into four piles.
Find $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$ of small quantities.

Using number facts

Know halves of even numbers to 24.
Know $2\times$, $5\times$ and $10\times$ division facts.
Begin to know $3\times$ division facts.

20	
?	?

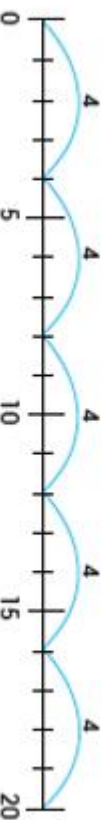
half of 20 is...

Multiplication and division are inverse operations. Right from the start children should be taught these as related operations. There are four number sentences (two using \times and two using \div which can be written to express the relationship between 5 and 9 and 45. It is key to a good understanding of division that $\square \times 5 = 45$ and $45 \div 5 = \square$ are seen as ways of expressing the same question.

\times Multiplication

Counting in steps ('Clever' counting)

Count in 2s, 3s, 4s, 5s, 8s and 10s, e.g. colour the multiples on a 1-100 grid or use hops along a landmarked line.



Doubling and halving

Find doubles to double 50 using partitioning.

Use doubling as a strategy in multiplying by 2.
e.g. 18×2 is double 18 (36).

$$\begin{array}{r} 80 \\ + 48 \\ \hline 16 = 96 \end{array}$$

Doubling and halving form the basis of mental \times & \div strategies.

Grouping

Recognise that multiplication is commutative, e.g. $4 \times 8 = 8 \times 4$.

Multiply multiples of 10 by single-digit numbers, e.g. $30 \times 8 = 240$.

Multiply friendly 2-digit numbers by single-digit numbers, e.g. 13×4 .

Using number facts

Know doubles to 20 and doubles of multiples of 5 to 100, e.g. double 45 is 90.

Know doubles of multiples of 5 to 100, e.g. double 85 is 170.

Know $2\times$, $3\times$, $4\times$, $5\times$, $8\times$, $10\times$ tables facts.

\times Written Multiplication

Build on partitioning to develop grid multiplication.

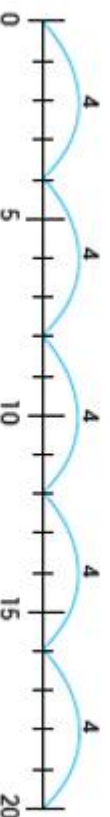
\times	20	3	=
4	80	12	92

Number facts must be memorised and used on a daily basis.

\div Division

Counting in steps ('Clever' counting)

Count in 2s, 3s, 4s, 5s, 9s and 10s by colouring numbers on the 1-100 grid or using a landmarked line.



Doubling and halving

Find half of even numbers to 100 using partitioning.

Use halving as a strategy in dividing by 2.
e.g. $36 \div 2$ is half of 36.

$$\begin{array}{r} 15 \\ + 36 \\ \hline 3 = 18 \end{array}$$

Grouping

Recognise that division is not commutative, e.g. $16 \div 8$ does not equal $8 \div 16$.

Relate division to multiplications 'with holes in', e.g. $\square \times 5 = 30$ is the same calculation as $30 \div 5 = ?$ thus we can count in in 5s to find the answer.

Divide multiples of 10 by single-digit numbers, e.g. $240 \div 8 = 30$.

Using number facts

Know halves of even numbers to 40.

28	?
?	?

Know halves of multiples of 10 to 200, e.g. half of 170 is 85.

Know $2\times$, $3\times$, $4\times$, $5\times$, $8\times$, $10\times$ division facts.

Use division facts to find unit and simple non-unit fractions of amounts within the times tables, e.g. $\frac{3}{4}$ of 48 is $3 \times (48 \div 4)$.

Multiplication and division are inverse operations. Right from the start children should be taught these as related operations. There are four number sentences (two using \times and two using \div which can be written to express the relationship between 5 and 9 and 45. It is key to a good understanding of division that $[] \times 5 = 45$ and $45 \div 5 = []$ are seen as ways of expressing the same question.

x Multiplication

Counting in steps (sequence)

Count in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 11s, 12s, 25s, 50s, 100s and 1000s.

Doubling and halving

Find doubles to double 100 and beyond using partitioning.

e.g. double 226.

$$\begin{array}{r} 226 \\ 400 + 40 + 12 = 452 \end{array}$$

Begin to double amounts of money.

e.g. £3.50 doubled is £7.

Use doubling as a strategy in multiplying by 2, 4 and 8.

e.g. $34 \times 4 =$ double 34 (68) doubled again (136).

Grouping

Use partitioning to multiply 2-digit numbers by single-digit numbers.

Multiply multiples of 100 by single-digit numbers using tables facts.

e.g. $400 \times 8 = 3200$.

Multiply using near multiples by rounding. e.g. 24×19 as $(24 \times 20) - 24$.

Using number facts

Know times tables up to 12×12 .

Facility in doubling and halving is key for mental \times and \div strategies.

÷ Division

Counting in steps (sequence)

Count in 2s, 3s, 4s, 5s, 6s, 7s, 8s, 9s, 10s, 11s, 12s, 25s, 50s, 100s and 1000s.

Doubling and halving

Find halves of even numbers to 200 and beyond using partitioning.

344	
172	172

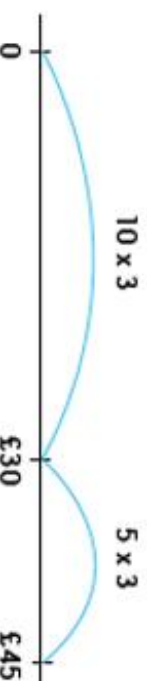
Begin to half amounts of money. e.g. £9 halved is £4.50.

Use halving as a strategy in dividing by 2, 4 and 8. e.g. $164 \div 4$ is half of 164 (82) halved again (41).

Grouping

Use multiples of 10 times the divisor to divide by numbers < 9 above the

tables facts. e.g. $45 \div 3$.



Divide multiples of 100 by single-digit numbers using division facts.

e.g. $3200 \div 8 = 4000$.

Using number facts

Know times tables up to 12×12 and all related division facts.

Use division facts to find unit and non-unit fractions of amounts within the times tables. e.g. $\frac{7}{8}$ of 56 is $7 \times (56 \div 8)$.

Stress that division is multiplication with 'holes' in.

Multiplication and division are inverse operations. Right from the start children should be taught these as related operations. There are four number sentences (two using \times and two using \div which can be written to express the relationship between 5 and 9 and 45. It is key to a good understanding of division that $\square \times 5 = 45$ and $45 \div 5 = \square$ are seen as ways of expressing the same question.

\times Written Multiplication

Use grid multiplication to multiply 3-digit by 1-digit numbers.

$$\begin{array}{r|rr|r} \times & 200 & 50 & 3 \\ 6 & 1200 & 300 & 18 \\ \hline & & & = 1518 \end{array}$$

Use a vertical written algorithm (ladder) to multiply 3-digit numbers by 1-digit numbers.

$$\begin{array}{r} 253 \\ \times 6 \\ \hline 1200 \\ 300 \\ 18 \\ \hline 1518 \end{array}$$

If children understand place value they can develop fluency.

\div Written Division

Written version of a mental method:

$$\square \times 3 = 86$$

$$20 \times 3 = 60$$

$$26$$

$$8 \times 3 = 24$$

$$2$$

$$86 \div 3 = \underline{28} \text{ r } 2$$

When faced with a calculation problem,
encourage children to ask...

★ Can I do this in my head?

★ Could I do this in my head using
drawings or jottings to help me?

★ Do I need to use a written method?

★ Should I use a calculator? *(only if is
necessary with the numbers involved)*



Also help children to estimate and then check
the answer.

Encourage them to ask...

Is the answer sensible?